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# FOURTH SEMESTER B.Sc. DEGREE (SUPPLEMENTARY/IMPROVEMENT) EXAMINATION, MAY 2016

(UG-CCSS)

Complementary Course

MM 4C 04—MATHEMATICS

Time: Three Hours

Maximum: 30 Weightage

### Section A

Answer all questions.

Each question carries a weightage of 1/4.

- 1. Is the equation  $y'' = \sqrt{y^{1^2} + 1}$  linear or non-linear?
- 2. Is  $y = e^{-x}$  a solution of y'' + y = 0?
- 3. Solve y'' + 7y = 0.
- 4. Find the Laplace Transform of  $f(t) = t^9$ .
- 5. Define the unit impulse function.
- 6. Find the inverse Laplace Transform of  $F(s) = \frac{2}{2s-3}$ .
- 7. Find the fundamental period of  $\cos 2\pi x$ .
- 8. Is the following function even or odd or neither  $x^2 \cos nx$ .
- 9. What is the 2 dimensional Laplace equation?
- 10. Define the Lipschitz condition.
- 11. What is an initial value problem?
- 12. State Simpson's rule.

 $(12 \times \frac{1}{4} = 3 \text{ weightage})$ 

### Section B

Answer all questions.

Each question carries a weightage of 1.

- 13. Find the Wronskean of the functions  $y_1 = x^2$  and  $y_2 = x^2 \ln x$ .
- 14. Find the solution of y'' + 4y' + 4y = 0.
- 15. Find the Laplace Transform of  $f(t) = \cosh 7t$ .

Turn over

- 16. Find the inverse Laplace Transform of  $F(s) = (s-2)^{-5}$ .
- 17. Is  $u = \sin ct \sin x$  a solution of the wave equation (with suitable c)?
- 18. Solve  $u_{xy} = u_x$ .
- 19. Solve  $u_y = u$ .
- 20. Show that  $f(x, y) = |\sin y| + x$  satisfies the Lipschitz condition with m = 1.
- 21. Apply Euler's method any compute  $y_1, y_2, \dots, y_5$  with h = 0.02, given y' = (y x)/(y + x), y(0) = 1.

 $(9 \times 1 = 9 \text{ weightage})$ 

## Section C

Answer any five questions. Each question carries a weightage of 2.

- 22. Solve  $y'' + y' = 2 + 2x + x^2$ , y(0) = 8, y'(0) = -1.
- 23. Solve  $x^2y'' + xy' + y = 0$ .
- 24. Find the Laplace Transform of F  $(t) = te^{-2t} \sin 2t$ .
- 25. State the convolution theorem and use it to evaluate the inverse h(t) of H  $(s) = s (s^2 + a^2)^{-2}$
- 26. Find the Fourier sine series of  $f(x) = \pi x$ ,  $0 < x < \pi$ .
- 27. Using Runge Kutta Method, find y when x = 0.2, given  $y' = \frac{y^2 x^2}{y^2 + x^2}$ , y(0) = 1.
- 28. Evaluate  $\int_{0}^{1} \frac{dx}{1+x^2}$  using Trapezoidal rule, taking h = 0.25.

 $(5 \times 2 = 10 \text{ weightage})$ 

#### Section D

Answer any **two** questions.

Each question carries a weightage of 4.

- 29. Solve  $y'' + y = \sec x$ .
- 30. Solve by the method of Laplace Transforms: y'' + y = t, y(0) = 1, y'(0) = -2.
- 31. Find the Fourier series expansion of  $f(x) = \frac{x^2}{2}$ ,  $-\pi < x < \pi$ . Hence show that

$$1 + \frac{1}{4} + \frac{1}{9} + \frac{1}{16} + \dots = \frac{\pi^2}{6}.$$

 $(2 \times 4 = 8 \text{ weightage})$