

D 12034

135824

(Pages : 3)

Name.....

Reg. No.....

## THIRD SEMESTER (CBCSS-UG) DEGREE EXAMINATION, NOVEMBER 2021

Mathematics

MTS 3C 03—MATHEMATICS - 3

(2019–2020 Admissions)

Time : Two Hours

Maximum : 60 Marks

## Section A

*Answer at least eight questions.**Each question carries 3 marks.**All questions can be attended**Overall Ceiling 24.*

~~✓~~ 1. Evaluate  $\int_0^1 (t\hat{i} + 3t^2\hat{j} + 4t^3\hat{k}) dt$ .

~~✓~~ 2. The position of a moving particle is  $\vec{r}(t) = t^2\hat{i} + t\hat{j} + t^3\hat{k}$ . Find velocity and acceleration of the particle at  $t = 2$ .

~~✓~~ 3. If  $z = e^{-x} \cos x$  find  $\frac{\partial^2 z}{\partial x \partial y}$ .

4. Find the level surface of  $F(x, y, z) = x^2 + y^2 + z^2$  passing through  $(1, 1, 1)$ .

~~✓~~ 5. Evaluate  $\oint_C x dx$ , where  $C$  is the circle  $x = \cos t, y = \sin t, 0 \leq t \leq 2\pi$ .

~~✓~~ 6. Show that  $\text{curl } \vec{r} = \vec{0}$ .

~~✓~~ 7. State Green's theorem in the plane.

~~✓~~ 8. Evaluate  $\int_0^3 \int_0^2 \int_0^1 xyz \, dx \, dy \, dz$ .

~~✓~~ 9. Write the equation of the circle with centre  $(1, 2)$  and radius 4 in the complex plane.

Turn over

135824

10. Find the value of  $i^{2i}$ .

11. Evaluate  $\int_C \frac{ze^z}{(z-3)} dz$ , where C is  $|z|=2$ .

12. Evaluate  $\oint_C \frac{dz}{z}$ , where C is  $|z|=1$ .

(8 × 3 = 24 marks)

### Section B

*Answer at least five questions.  
Each question carries 5 marks.  
All questions can be attended.  
Overall Ceiling 25.*

13. Use chain rule to find  $\frac{dw}{dx}$  at  $(0,1,2)$  for  $w = xy + yz$ ;  $x = \cos x$ ,  $y = \sin x$ ,  $z = e^x$ .

14. Find the directional derivative of  $f(x,y) = \sqrt{x^2y + 2y^2z}$  at  $(-2,2,1)$  in the direction of the negative z-axis.

15. Find the area lying between the parabola  $y = 4x - x^2$  and the line  $y = x$  using double integrals.

16. Use polar coordinates to evaluate  $\int_0^2 \int_{-\sqrt{8-x^2}}^{\sqrt{8-x^2}} \frac{1}{5+x^2+y^2} dy dx$ .

17. Show that  $f(z) = (2x^2 + y) + i(y^2 - x)$  is not analytic at any point.

18. Evaluate  $\oint_C \frac{5z+7}{z^2+2z-3} dz$ , where C is the circle  $|z-2|=2$ . *Ans*

19. Evaluate  $\int \operatorname{Re} z dz$  along a line segment from  $z=0$  to  $z=1+2i$ .

(5 × 5 = 25 marks)

**135824**

3

**D 12034**

### **Section C**

*Answer any one question.  
The question carries 11 marks.*

20. Let  $\vec{F}(x, y, z) = z\hat{j} + z\hat{k}$  represents the flow of a liquid. Find the flux of  $\vec{F}$  through the surface S given by that portion of the plane  $z = 6 - 3x - 2y$  in the first octant oriented upward.
21. Use triple integrals to find the volume of the solid with in the cylinder  $x^2 + y^2 = 9$  and between the planes  $z = 1$  and  $x + z = 5$ .  $(1 \times 11 = 11 \text{ marks})$